

### Metallic and Ionic Solids

### Types of Solids

*Table 13.6*

<u>TYPE</u>	<u>EXAMPLE</u>	<u>FORCE</u>
Ionic	NaCl, CaF <sub>2</sub> , ZnS	Ion-ion
Metallic	Na, Fe	Metallic
Molecular	Ice, I <sub>2</sub>	Dipole Ind. dipole
Network	Diamond Graphite	Extended covalent

### Properties of Solids

1. Molecules, atoms or ions locked into a **CRYSTAL LATTICE**
2. Particles are **CLOSE** together
3. **STRONG IM** forces
4. Highly ordered, rigid, incompressible

ZnS, zinc sulfide

### Crystal Lattices

- Regular 3-D arrangements of equivalent **LATTICE POINTS** in space.
- Lattice points define **UNIT CELLS**
  - smallest repeating internal unit that has the symmetry characteristic of the solid.

### Cubic Unit Cells

There are 7 basic crystal systems, but we are only concerned with **CUBIC**.

All sides equal length

All angles are 90 degrees

Cubic  
 $a = b = c$   
 $\alpha = \beta = \gamma = 90^\circ$

### Cubic Unit Cells of Metals

*Figure 13.27*

Simple cubic (SC)

Body-centered cubic (BCC)

Face-centered cubic (FCC)

### Cubic Unit Cells of Metals 7

*Figure 13.27*

Simple cubic

Body-centered cubic

Face-centered cubic

### Units Cells for Metals 8

H																	He
Li	Be											B	C	N	O	F	Ne
Na	Mg											Al	Si	P	S	Cl	Ar
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe
Cs	Ba	La	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn
Fr	Ra	Ac															

Figure 13.28

Simple cubic

Cubic close packing  
(Face-centered cubic)

Body-centered cubic

Hexagonal close packing

### Simple Cubic Unit Cell 9

*Figure 13.26*

Each face is part of two cubes

Each edge is part of four cubes

Each corner is part of eight cubes

- E atom is at a corner of a unit cell and is shared among 8 unit cells.
- Each edge is shared with 4 cells
- Each face is part of two cells.

### Body-Centered Cubic Unit Cell 10

### Face Centered Cubic Unit Cell 11

Atom at each cube corner plus atom in each cube face.

### Atom Packing in Unit Cells 12

Assume atoms are hard spheres and that crystals are built by PACKING of these spheres as efficiently as possible.

### Atom Packing in Unit Cells 13

Assume atoms are hard spheres and that crystals are built by **PACKING** of these spheres as efficiently as possible.

### Atom Packing in Unit Cells 14

(a) Hexagonal close-packing (hcp)

(b) Cubic close-packing = face centered cubic (fcc)

**Atom Packing in Unit Cells**

### Crystal Lattices— Packing of Atoms or Ions 15

- FCC is more efficient than either BC or SC.
- Leads to layers of atoms.

### Crystal Lattices— Packing of Atoms or Ions 16

Packing of  $C_{60}$  molecules. They are arranged at the lattice points of a FCC lattice.

### Number of Atoms per Unit Cell 17

Unit Cell Type	Net Number Atoms
SC	1
BCC	2
FCC	4

Simple cubic

Body-centered cubic

Face-centered cubic

### Atom Sharing at Cube Faces and Corners 18

Atom shared in corner --> 1/8 inside each unit cell

Atom shared in face --> 1/2 inside each unit cell

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### Simple Ionic Compounds

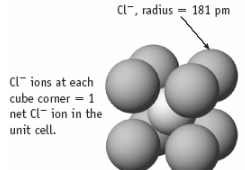
Lattices of many simple ionic solids are built by taking a SC or FCC lattice of ions of one type and placing ions of opposite charge in the holes in the lattice.

**EXAMPLE:** CsCl has a SC lattice of Cs<sup>+</sup> ions with Cl<sup>-</sup> in the center.

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### Simple Ionic Compounds

Cl<sup>-</sup>, radius = 181 pm



Cl<sup>-</sup> lattice and Cs<sup>+</sup> in lattice hole

CsCl unit cell has a SC lattice of Cl<sup>-</sup> ions with Cs<sup>+</sup> in the center.

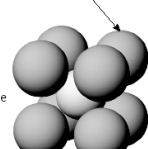
1 unit cell has 1 Cs<sup>+</sup> ion plus (8 corners)(1/8 Cl<sup>-</sup> per corner) = 1 net Cl<sup>-</sup> ion.

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### Two Views of CsCl Unit Cell

- Lattice can be SC lattice of Cl<sup>-</sup> with Cs<sup>+</sup> in hole
- OR SC lattice of Cs<sup>+</sup> with Cl<sup>-</sup> in hole
- Either arrangement leads to formula of 1 Cs<sup>+</sup> and 1 Cl<sup>-</sup> per unit cell


Cl<sup>-</sup>, radius = 181 pm



Cl<sup>-</sup> ions at each cube corner = 1 net Cl<sup>-</sup> ion in the unit cell.

Cl<sup>-</sup> lattice and Cs<sup>+</sup> in lattice hole

Cs<sup>+</sup>, radius = 165 pm



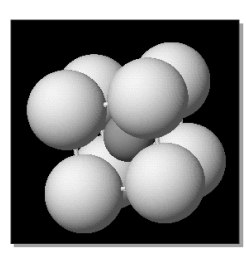
One Cs<sup>+</sup> ion at each cube corner gives one net Cs<sup>+</sup> ion in the unit cell.

Cs<sup>+</sup> lattice and Cl<sup>-</sup> in lattice hole

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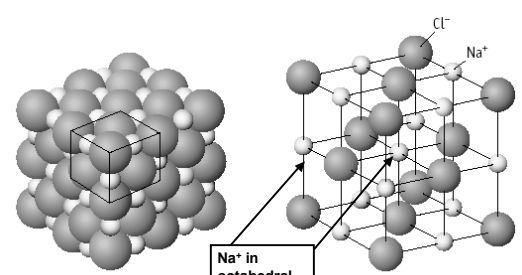
### Simple Ionic Compounds

Salts with formula MX can have SC structure — but not salts with formula MX<sub>2</sub> or M<sub>2</sub>X



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### NaCl Construction



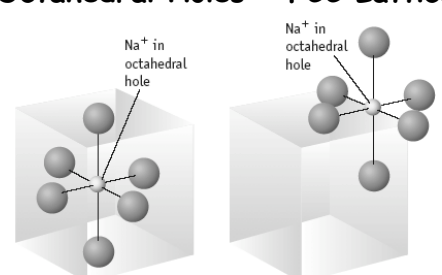
FCC lattice of Cl<sup>-</sup> with Na<sup>+</sup> in holes

Na<sup>+</sup> in octahedral holes

NaCl unit cell (expanded)

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### Octahedral Holes - FCC Lattice



Na<sup>+</sup> in octahedral hole

Na<sup>+</sup> in octahedral hole

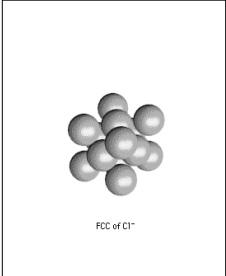
1 hole of this kind in the center of the unit cell

12 holes of this kind in the 12 edges of the unit cell (a net of 3 holes)

Octahedral holes in a face-centered lattice

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### The Sodium Chloride Lattice



FCC of Cl<sup>-</sup>

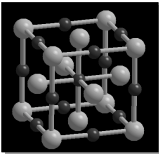
Na<sup>+</sup> ions are in **OCTAHEDRAL** holes in a face-centered cubic lattice of Cl<sup>-</sup> ions.

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### The Sodium Chloride Lattice

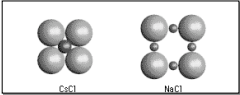
Many common salts have FCC arrangements of anions with cations in **OCTAHEDRAL HOLES** — e.g., salts such as  $CA = NaCl$

- FCC lattice of anions ----> 4 A<sup>-</sup>/unit cell
- C<sup>+</sup> in octahedral holes ----> 1 C<sup>+</sup> at center + [12 edges • 1/4 C<sup>+</sup> per edge] = 4 C<sup>+</sup> per unit cell



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### Comparing NaCl and CsCl

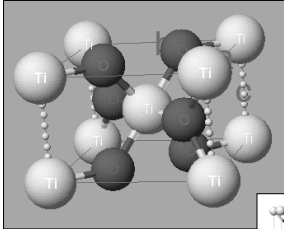


CsCl      NaCl

- Even though their formulas have one cation and one anion, the lattices of CsCl and NaCl are different.
- The different lattices arise from the fact that a Cs<sup>+</sup> ion is much larger than a Na<sup>+</sup> ion.

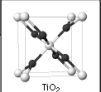
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### Common Ionic Solids



Titanium dioxide, TiO<sub>2</sub>

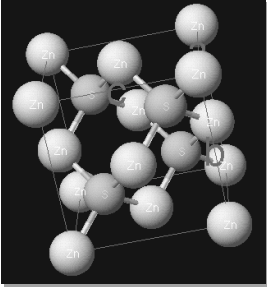
There are 2 net Ti<sup>4+</sup> ions and 4 net O<sup>2-</sup> ions per unit cell.



TiO<sub>2</sub>

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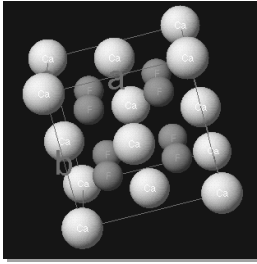
### Common Ionic Solids



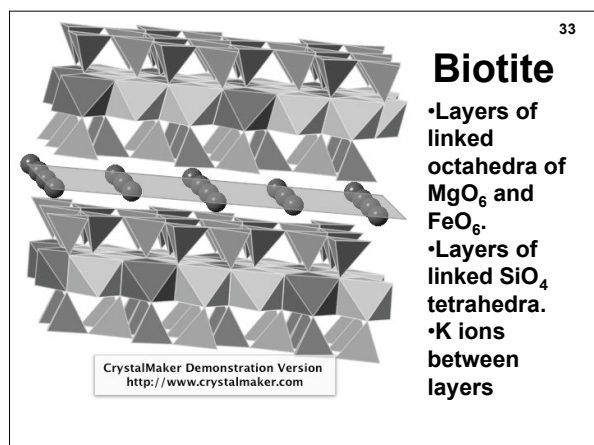
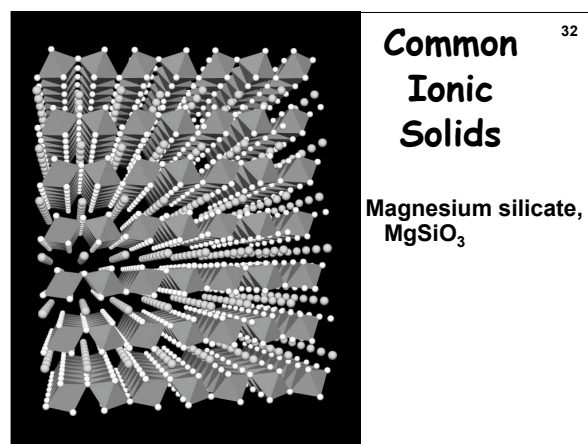
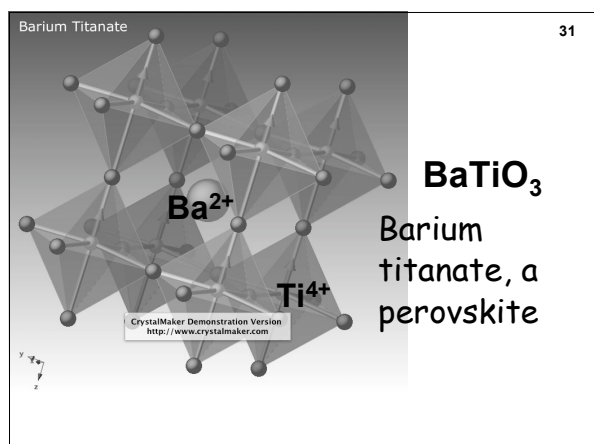
- Zinc sulfide, ZnS
- The S<sup>2-</sup> ions are in **TETRAHEDRAL** holes in the Zn<sup>2+</sup> FCC lattice.
- This gives 4 net Zn<sup>2+</sup> ions and 4 net S<sup>2-</sup> ions.

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### Common Ionic Solids



- Fluorite or CaF<sub>2</sub>
- FCC lattice of Ca<sup>2+</sup> ions
- This gives 4 net Ca<sup>2+</sup> ions.
- F<sup>-</sup> ions in all 8 tetrahedral holes.
- This gives 8 net F<sup>-</sup> ions.



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### Finding the Lattice Type

**PROBLEM** Al has density = 2.699 g/cm<sup>3</sup> and Al radius = 143 pm. Verify that Al is FCC.

**SOLUTION**

1. Calc. unit cell volume

$V = (\text{cell edge})^3$

Edge distance comes from face diagonal.

Diagonal distance =  $\sqrt{2} \cdot \text{edge}$

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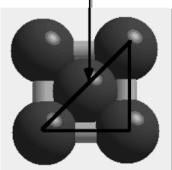
### Finding the Lattice Type

**PROBLEM** Al has density = 2.699 g/cm<sup>3</sup> and Al radius = 143 pm. Verify that Al is FCC.

**SOLUTION**

$V = (\text{cell edge})^3$  and face diagonal =  $\sqrt{2} \cdot \text{edge}$

$(\text{Diagonal})^2 = 2 (\text{edge})^2$



Therefore,  
Diag =  $\sqrt{2} \cdot (\text{edge})$

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### Finding the Lattice Type

**PROBLEM** Al has density = 2.699 g/cm<sup>3</sup> and Al radius = 143 pm. Verify that Al is FCC.

**SOLUTION**

Here diagonal = 4 • radius of Al = 572 pm

Therefore, edge = 572 pm /  $\sqrt{2}$  = 404 pm

In centimeters, edge = 4.04 x 10<sup>-8</sup> cm

So, V of unit cell = (4.04 x 10<sup>-8</sup> cm)<sup>3</sup>

$V = 6.62 \times 10^{-23} \text{ cm}^3$

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### Finding the Lattice Type

**PROBLEM** Al has density = 2.699 g/cm<sup>3</sup> and Al radius = 143 pm. Verify that Al is FCC.

**SOLUTION**

2. Use V and density to calc. mass of unit cell from

$$\text{DENS} = \text{MASS} / \text{VOL}$$

$$\text{Mass} = \text{density} \cdot \text{volume}$$

$$= (6.62 \times 10^{-23} \text{ cm}^3)(2.699 \text{ g/cm}^3)$$

$$= 1.79 \times 10^{-22} \text{ g/unit cell}$$

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### Finding the Lattice Type

**PROBLEM** Al has density = 2.699 g/cm<sup>3</sup> and Al radius = 143 pm. Verify that Al is FCC.

**SOLUTION**

3. Calculate number of Al per unit cell from mass of unit cell.

$$\text{Mass 1 Al atom} = \frac{26.98 \text{ g}}{\text{mol}} \cdot \frac{1 \text{ mol}}{6.022 \times 10^{23} \text{ atoms}}$$

$$1 \text{ atom} = 4.480 \times 10^{-23} \text{ g, so}$$

$$\frac{1.79 \times 10^{-22} \text{ g}}{\text{unit cell}} \cdot \frac{1 \text{ atom}}{4.480 \times 10^{-23} \text{ g}} = 3.99 \text{ Al atoms/unit cell}$$

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### Number of Atoms per Unit Cell

How can there be 4 atoms in a unit cell?

1. Each corner Al is 1/8 inside the unit cell.

$$8 \text{ corners } (1/8 \text{ Al per corner}) = 1 \text{ net Al}$$

2. Each face Al is 1/2 inside the cell

$$6 \text{ faces } (1/2 \text{ per face}) = 3 \text{ net Al's}$$

